

PREDISTORTED WAVEGUIDE FILTERS
FOR USE IN
COMMUNICATIONS SYSTEMS

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Predistortion is a standard technique for correcting the effects of energy dissipation in filters, making their response conform to that of ideal filters. The problem of dissipation is particularly noticeable in narrow-band bandpass filters used in microwave communications systems. Dissipation makes the passband edges slump downward, as shown in Figure 1, which can cause distortion and intermodulation.

In predistorting a filter, we allow for dissipation in the initial design. A response approximating the ideal response can be approximated at the price of increased insertion loss. The flat response of predistorted filters is advantageous when used in high-capacity microwave communications systems; however, the filters have an additional property which makes them especially attractive for certain applications in microwave communications systems.

Consider the diplexing scheme shown in Figure 2, in which several filters tuned to different frequencies are connected to a common transmission line with circulators. This scheme works quite well if there is a wide spacing between the frequencies to be separated. When the frequencies are close together, however, the differential time delay of a signal reflecting off a filter tuned to a nearby frequency will be affected. Frequencies closer to the filter frequency will have more group time delay, as shown in Figure 3. Here, we see the differential group delay of a signal reflected off a 7-cell, 37-MHz bandwidth, maximally-flat filter. The signal is 60 MHz above and below the filter frequency. The differential delay across a 24-MHz bandwidth amounts to 3 nanoseconds, which can cause severe intermodulation distortion and crosstalk on high-capacity communications systems.

NOTES

It has been found that this group delay tilt is inversely proportional to the loaded Q of the end cavity of the filter from which the signal reflects. It happens that predistorted waveguide filters of the type described are asymmetrical with regard to end-cavity Q 's. The cavity on one end will be higher in Q and the cavity on the other end lower in Q than that of a conventional, maximally-flat, filter end cavity. By arranging the filter such that the high Q cavity is always next to the circulator, it is possible to reduce the reflected group differential delay to 1 nanosecond, as shown in Figure 4.

This reduced delay tilt is much easier to correct, and the additional advantage of amplitude flatness within the passband makes this type of filter attractive for high-density communications systems.

Predistorted waveguide bandpass filters can be designed using a lowpass prototype filter, just as can conventional Butterworth and Tchebyscheff waveguide filters.

The procedure for designing a bandpass filter is as follows:

1. Calculate or estimate unloaded Q_u of filter resonator.
2. Define $\delta = \frac{f}{Q_u BW}$, where f is the frequency and BW is the 3-db bandwidth.
3. Synthesize the desired lowpass prototype filter, with its poles shifted toward the $j\omega$ axis by the amount, δ .

For example, suppose we want to design a 5-cell waveguide bandpass filter with the following characteristics:

Response:	Maximally flat
Frequency:	6450 MHz
3-db Bandwidth:	44 MHz

The unloaded Q of the filter cavities can be determined from the insertion loss of an existing filter using the relation given by Cohn¹:

$$L = 4.343 \frac{w_1'}{W} \sum_{i=1}^n \frac{g_i}{Q_i} \quad (1)$$

where:

- L = insertion loss in db
- w_1' = cutoff frequency of lowpass prototype filter
- W = fractional bandwidth
- Q_i = the unloaded Q of the ith cavity
- g_i = the ith element value of lowpass prototype

Suppose, for instance, we have a 5-cell, conventional, maximally-flat filter which has a 0.762-db insertion loss at 6450 MHz and a 3-db bandwidth of 35 MHz. Then, Q_u , if it is the same for all cavities, = $\frac{4.343 \times 6450}{35 \times 0.762}$ (0.618 + 1.618 + 2.000 + 1.618 + 0.618) = 6800. Then, $\delta = \frac{6450}{6800 \times 44} = 0.0216$.

Now, shift the poles of a 5-element, maximally-flat, lowpass prototype toward the $j\omega$ axis by an amount, 0.0216, as shown in Figure 5. These poles are now used to synthesize a doubly-terminated LC filter. The lowpass prototype is shown in Figure 6.

Finally, to determine the waveguide filter dimensions, we use the formulas by Cohn²:

$$X_{01} = \frac{\sqrt{\frac{\Omega}{g_1}}}{1 - \frac{\Omega}{g_1}} \quad X_{ij} = \frac{\frac{\Omega}{\sqrt{g_i g_j}}}{1 - \frac{\Omega}{g_i g_j}} \quad X_{56} = \frac{\sqrt{\frac{\Omega}{g_5 g_6'}}}{1 - \frac{\Omega}{g_5 g_6'}} \quad (2)$$

$$\phi_j = 180^\circ - \frac{1}{2} [\tan^{-1} (2X_{ij}) + \tan^{-1} (2X_{jk})]$$

where:

$$\Omega = \pi \frac{\lambda g_1 - \lambda g_2}{\lambda g_1 + \lambda g_2} = 0.01930 \quad \begin{array}{l} \lambda g_1 = \lambda g @ 6450 - 22 \text{ MHz} \\ \lambda g_2 = \lambda g @ 6450 + 22 \text{ MHz} \end{array}$$

$$\begin{array}{ll} g_1 = 1.4940 & g_4 = 0.8600 \\ g_2 = 1.4697 & g_5 = 0.5541 \\ g_3 = 2.4214 & g_6 = 1.3622 \quad g_6' = \frac{\Omega}{g_6} \end{array}$$

From these equations, we find:

$$\begin{array}{ll} X_{01} = 0.1151 & \phi_1 = 172.77^\circ \\ X_{12} = 0.01303 & \phi_2 = 178.67^\circ \\ X_{23} = 0.01023 & \phi_3 = 178.65^\circ \\ X_{34} = 0.01338 & \phi_4 = 177.63^\circ \\ X_{45} = 0.02798 & \phi_5 = 166.11^\circ \\ X_{56} = 0.2287 & \end{array}$$

Table 1 gives lowpass prototype element values for 5- and 7-element, maximally-flat filters, for different values of δ .

The synthesis procedure used is the conventional, doubly-terminated, LC network theory, as described, for instance, by Guillemin³.

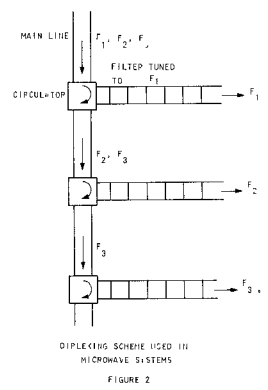
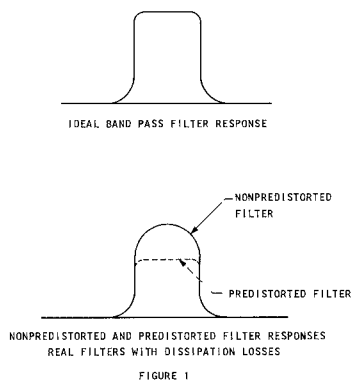
The predistorted bandpass filters described have the advantages of a more ideal response and of reduced differential group delay of signals reflected off the filter; however, the filters have two disadvantages which have to be considered. First, the filters have a large VSWR in the center of the passband. The flatness of response is achieved only by reflecting power in the passband center, which is not absorbed as much as power toward the passband edges. This means the filter has to be isolated from unmatched

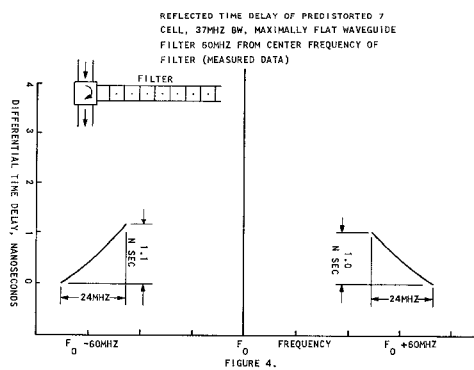
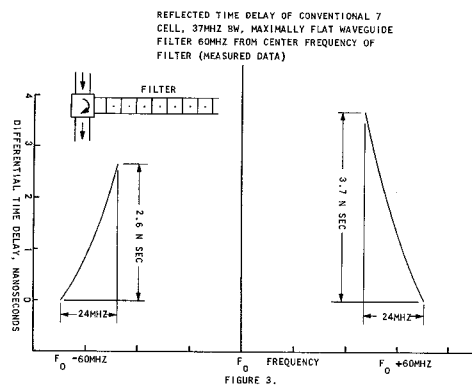
sources and loads. A second disadvantage is the high sensitivity of the element values. The filter appears to be more sensitive to incorrect element values than conventional, maximally-flat filters.

TABLE 1

5-ELEMENT DATA							
δ	R_1	R_2	R_3	R_4	R_5	R_6	
0.005	1.1745	1.7585	2.0230	1.0878	0.4741	1.1144	
0.010	1.2940	1.8574	2.1417	0.9970	0.4950	1.1945	
0.015	1.3871	1.9705	2.2605	0.9305	0.5194	1.2675	
0.020	1.4691	1.4950	2.3818	0.8758	0.5454	1.3392	
0.025	1.5452	1.4223	2.5068	0.8285	0.5725	1.4114	
0.030	1.6181	1.3569	2.6366	0.7861	0.6017	1.4849	
0.035	1.6892	1.2959	2.7716	0.7478	0.6320	1.5605	
0.040	1.7595	1.2385	2.9132	0.7124	0.6640	1.6387	
0.045	1.8299	1.1844	3.0610	0.6795	0.6978	1.7199	
0.050	1.9008	1.1330	3.2177	0.6486	0.7335	1.8045	

7-ELEMENT DATA								
δ	R_1	R_2	R_3	R_4	R_5	R_6	R_7	R_8
0.005	1.2521	1.8015	2.3313	1.6182	1.5395	0.6741	0.3261	1.1936
0.010	1.4311	1.4647	2.5708	1.2648	1.6783	0.5983	0.3543	1.3219
0.015	1.5765	1.3511	2.8037	1.1510	1.8199	0.5434	0.3846	1.4441
0.020	1.7088	1.2525	3.0409	1.0574	1.9672	0.4989	0.4158	1.5699
0.025	1.8255	1.1648	3.2878	0.9769	2.1215	0.4609	0.4487	1.6925
0.030	1.9404	1.0824	3.5400	0.9057	2.2870	0.4274	0.4838	1.8258
0.035	2.0859	1.0129	3.8245	0.8416	2.4631	0.3974	0.5214	1.9655
0.040	2.2137	0.9460	4.1204	0.7834	2.6523	0.3701	0.5619	2.1129





REFERENCES

1. Cohn, S. B., "Dissipation Loss in Multiple Coupled Resonator Filters," Proceedings of IRE, August 1959.
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3. Guillemin, E. A., Synthesis of Passive Networks, John Wiley & Sons, 1957.

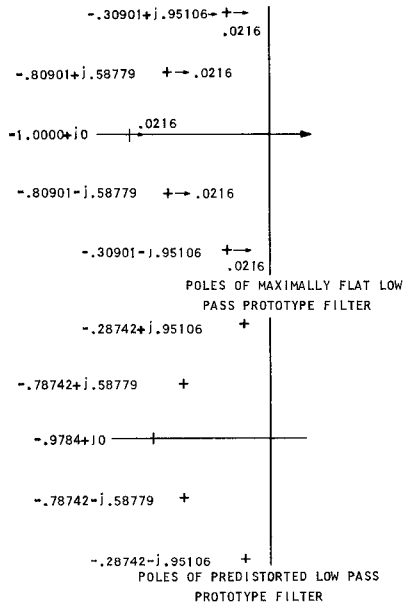


FIGURE 5.

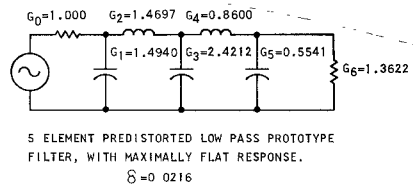


FIGURE 6